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## Crystal Structure

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# $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$ : a calcium europium tin oxide with a novel structure 

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A new quaternary compound in the $\mathrm{Ca}-\mathrm{Eu}-\mathrm{Sn}-\mathrm{O}$ system, namely calcium europium tin heptaoxide, $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$, was prepared by solid-state reaction at 2073 K . All atoms in the structure are on $4 i$ special positions (on mirrors) in space group $C 2 / m . \mathrm{Ca} / \mathrm{Eu}$ sites are situated within two O octahedra and within two sevenfold coordination sites surrounded by O-capped trigonal prisms. A $\mathrm{Ca} / \mathrm{Eu} / \mathrm{Sn}$ site is coordinated by five O atoms. The structural formula can be represented as $\left(\mathrm{Ca}_{0.28} \mathrm{Eu}_{0.72}\right)\left(\mathrm{Ca}_{0.16} \mathrm{Eu}_{0.84}\right)\left(\mathrm{Ca}_{0.46} \mathrm{Eu}_{0.54}\right)\left(\mathrm{Ca}_{0.28} \mathrm{Eu}_{0.72}\right)\left(\mathrm{Ca}_{0.32^{-}}\right.$ $\left.\mathrm{Eu}_{0.18} \mathrm{Sn}_{0.50}\right) \mathrm{O}_{7}$. The crystal structure is a new type and is related to the structure of B-form $\mathrm{Eu}_{2} \mathrm{O}_{3}$.

## Comment

Recently, a new quaternary oxide, $\mathrm{Ca}_{0.8} \mathrm{Y}_{2.4} \mathrm{Sn}_{0.8} \mathrm{O}_{6}$, isostructural with $\mathrm{Mg}_{3} \mathrm{TeO}_{6}$ and a member of the $\mathrm{Ca}-\mathrm{Y}-\mathrm{Sn}-\mathrm{O}$ system, was prepared by solid-state reaction (Kaminaga et al., 2006). In an attempt to substitute Eu atoms for all Y atoms in the compound, a mixture of the compound, with the $\mathrm{Mg}_{3} \mathrm{TeO}_{6}$ type structure, and $\mathrm{CaSnO}_{3}$, with a perovskite-type structure, was prepared at 1673 K . In order to form single crystals, we
heated the sample to 2073 K and in fact obtained the title new quaternary compound with a new structure in the $\mathrm{Ca}-\mathrm{Eu}-\mathrm{Sn}-$ O system, and present its structure here.

A Ca:Eu:Sn molar ratio of $3: 6: 1$ was measured for the single crystals obtained using an energy-dispersive X-ray (EDX) analyser on a scanning electron microscope. The proportions of Eu and Sn in the crystals were lower than those in the starting materials ( $\mathrm{Ca}: \mathrm{Eu}: \mathrm{Sn}=1: 3: 1$ ).

All metal $(M)$ and O atoms are located on mirrors ( $4 i$ special positions) with $y=0$ and $\frac{1}{2}$. After obtaining a starting model using SIR2004 (Burla et al., 2005), Eu atoms were tentatively placed at all $M$ sites for the first step and their positions were refined. The bond-valence sums for the $M$ sites, calculated with the bond lengths of $M-\mathrm{O}$ and the bondvalence parameter of $\mathrm{Eu}^{\mathrm{III}}-\mathrm{O}^{\mathrm{II}}=2.076$ (Brese \& O'Keeffe, 1991), were 2.771, 2.943, 2.694, 2.947 and 3.785, respectively. Based on this information, we set four mixed sites of Ca and Eu atoms $(\mathrm{Ca} / \mathrm{Eu})$, where the bond-valence sums were below 3 , and a $\mathrm{Ca} / \mathrm{Eu} / \mathrm{Sn}$ site with the bond valence above 3 . In accordance with the composition analysed by EDX, the occupancy parameter of Sn at the $\mathrm{Ca} / \mathrm{Eu} / \mathrm{Sn}$ site was fixed at 0.5 . The occupancy parameters of the Ca and Eu atoms at the sites Ca1/Eu1, Ca2/Eu2, Ca3/Eu3, Ca4/Eu4 and Ca5/Eu5/Sn5 were refined to $0.278(3) / 0.722(3), \quad 0.165(3) / 0.835(3)$, 0.458 (3)/0.542 (3), 0.281 (3)/0.719 (3) and $0.32(19) / 0.18$ (5), respectively. The overall Ca:Eu:Sn molar ratio, calculated with these values, was in good agreement with the ratio from the EDX analysis ( $\mathrm{Ca}: \mathrm{Eu}: \mathrm{Sn}=3: 6: 1$ ).

Fig. 1 shows the atomic arrangement around the $M$ sites with $\mathrm{Ca} 1 / \mathrm{Eu} 1$ - and $\mathrm{Ca} 2 / \mathrm{Eu} 2$-centred oxygen trigonal prisms. The Ca1/Eu1 and Ca2/Eu2 sites are surrounded by six nearest O atoms which form trigonal prisms. The $M-\mathrm{O}$ bond lengths in the $\mathrm{Ca} 1 / \mathrm{Eu} 1-\mathrm{and} \mathrm{Ca} 2 / \mathrm{Eu} 2-\mathrm{centred}$ prisms are 2.272 (6)2.528 (4) and 2.288 (3)-2.488 (4) Å, respectively. The secondnearest neighbour O atoms, capping the widest rectangular plane of each trigonal prism, are located 2.606 (7) Å from Ca1/ Eu 1 and 2.716 (5) $\AA$ from Ca2/Eu2. Consequently, the corresponding metal atom sites are best described as seven-coordinated. The O atoms surrounding the Ca3/Eu3 and Ca4/Eu4 sites form distorted octahedra. The $M-\mathrm{O}$ bond lengths are


Figure 1
The O -atom coordination around five $M$ sites in the structure of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$, showing $\mathrm{Ca} 1 / \mathrm{Eu} 1-\mathrm{and} \mathrm{Ca} 2 / \mathrm{Eu} 2$-centred oxygen trigonal prisms. Displacement ellipsoids are drawn at the $50 \%$ probability level. [Symmetry codes as in Table 1; additionally: (x) $-x+\frac{1}{2},-y+\frac{1}{2}, z ;(\mathrm{xi}) x+\frac{1}{2}, y-\frac{1}{2} z+1$.]


Figure 2
The $M$-atom coordination around O sites. Displacement ellipsoids are drawn at the $50 \%$ probability level. [Symmetry codes as in Table 1; additionally: (xi) $x+\frac{1}{2}, y-\frac{1}{2}, z+1$; (xii) $x+\frac{1}{2}, y-\frac{1}{2}, z$; (xiii) $x+\frac{1}{2}, y+\frac{1}{2}, z$; (xiv) $-x+\frac{1}{2},-y+\frac{1}{2},-z$; (xv) $-x+\frac{1}{2},-y+\frac{1}{2},-z+1$.]
2.213 (5)-2.541 (4) (Ca3/Eu3-O) and 2.250 (3)-2.580 (4) $\AA$ (Ca4/Eu4-O). Second-nearest neighbour O atoms are located at distances of 3.204 (7) (Ca3/Eu3-O1) and 3.311 (9) $\AA(\mathrm{Ca} / \mathrm{Eu} 4-\mathrm{O} 6) \AA$. The $\mathrm{Ca} 5 / \mathrm{Eu} 5 / \mathrm{Sn} 5$ site is coordinated by five O atoms, with bond lengths ranging from 2.118 (3) to 2.386 (9) $\AA$. The second-nearest neighbour O atom is 3.236 (5) $\AA$ from the $\mathrm{Ca} 5 / \mathrm{Eu} 5 / \mathrm{Sn} 5$ site.

The arrangement of $M$ atoms around O atoms is shown in Fig. 2. Atoms O4, O5, O6 and O7 are surrounded by four $M$ atoms, atom O 1 by five $M$ atoms, and atoms O 2 and O 3 by six $M$ atoms. The equivalent isotropic displacement parameter of atom O6 is almost twice those of the other O atoms. This may result from the difference in the coordination environment around O6 compared with the others. Each O atom, except O6 is located inside an $M$ polyhedron, while atom $\mathrm{O6}^{\mathrm{xv}}$ lies in a plane formed by Ca1/Eu1 $1^{\text {xii }}, \mathrm{Ca} 1 / \mathrm{Eu} 1^{\text {xiii }}$ and $\mathrm{Ca} 5 / \mathrm{Eu} 5 / \mathrm{Sn} 5^{\text {vi }}$ (symmetry codes as in Fig. 2 and Table 1). These three sites are parts of a distorted tetrahedron which is completed by $\mathrm{Ca} 5 /$ Eu5/Sn5 ${ }^{\mathrm{xi}}$. The direction of the ellipsoid long axis is toward the $\mathrm{Ca} 4 / \mathrm{Eu} 4^{\mathrm{vi}}$ and $\mathrm{Ca} 5 / \mathrm{Eu} 5 / \mathrm{Sn} 5^{\mathrm{xi}}$ sites, with distances of 3.311 (9) and 2.386 (9) A, respectively.

We could not find any isotypic compound in the Inorganic Crystal Structure Database (ICSD, 2005). However, the crystal structure of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$ can be related to the structure of the B -form of $\mathrm{Eu}_{2} \mathrm{O}_{3}$. This form is a midtemperature monoclinic phase which is stable from 1423 to 2273 K, between the high-temperature A-form hexagonal phase and the low-temperature C-form cubic phase (Yakel, 1979). The space group of the B-form of $\mathrm{Eu}_{2} \mathrm{O}_{3}$ is the same $(C 2 / m)$ as that of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$. The refined unit-cell parameters of B-form $\mathrm{Eu}_{2} \mathrm{O}_{3}$ are $a=14.1105$ (2) $\AA$, $b=$ 3.6021 (1) $\AA, c=8.8080$ (2) $\AA$ and $\beta=100.037(1)^{\circ}$, and the unit-cell volume is 440.84 (3) $\AA^{3}$. In the structure of B-form $\mathrm{Eu}_{2} \mathrm{O}_{3}$, there are three Eu sites and five O sites, all of which are also on $4 i$ special positions with $y=0$ and $\frac{1}{2}$. The $b$ axis lengths of B -form $\mathrm{Eu}_{2} \mathrm{O}_{3}$ and $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$ [3.6294 (2) $\AA$ ] are similar. The coordination environments of Eu 1 and Eu 2 are similar to those of $\mathrm{Ca} 1 / \mathrm{Eu} 1$ and $\mathrm{Ca} 2 / \mathrm{Eu} 2$ in


Figure 3
(a) The extended structure of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$, illustrated with $\mathrm{Ca} 1 / \mathrm{Eu} 1-$ and $\mathrm{Ca} 2 / \mathrm{Eu} 2$-centred oxygen trigonal prisms. (b) The structure of B-form $\mathrm{Eu}_{2} \mathrm{O}_{3}$, illustrated with Eu1- and Eu2-centred oxygen trigonal prisms.
$\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$. The $\mathrm{Eu} 1-\mathrm{O}$ bond lengths are 2.290 (2)2.537 (2) (prism) and 2.656 (4) A (cap), and the Eu2-O bond lengths are 2.288 (2)-2.462 (2) (prism) and 2.7394 (2) $\AA$ (cap). As with the $\mathrm{Ca} 3 / \mathrm{Eu} 3$ and $\mathrm{Ca} 4 / \mathrm{Eu} 4$ sites of the present structure of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$, in B -form $\mathrm{Eu}_{2} \mathrm{O}_{3}$, the Eu 3 atoms are in a distorted O octahedron, with $\mathrm{M}-\mathrm{O}$ bond lengths ranging from 2.239 (2) to 2.544 (1) $\AA$. The second-nearest neighbour O atom is 3.133 (4) $\AA$ from Eu3.

The extended structure of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$ is illustrated in Fig. 3(a), with $\mathrm{Ca} 1 / \mathrm{Eu} 1-$ and $\mathrm{Ca} 2 / \mathrm{Eu} 2$-centred oxygen trigonal prisms. The structure of B-form $\mathrm{Eu}_{2} \mathrm{O}_{3}$ is shown in Fig. 3(b), with Eu1- and Eu2-centred oxygen trigonal prisms. As shown in Fig. 4, pairs of $\mathrm{Ca} 1 / \mathrm{Eu} 1$-centred prisms in $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$, sharing $\mathrm{O} 4-\mathrm{O} 4^{i}$ edges lying in the plane ( $\overline{5} 01$ ), stack parallel to the $b$-axis direction by sharing $\mathrm{O} 3-\mathrm{O}^{\mathrm{ii}}$ edges. Pairs of $\mathrm{Ca} 2 /$ Eu2-centred prisms, which share $\mathrm{O} 7^{\mathrm{iii}}-\mathrm{O} 7^{\mathrm{iv}}$ and $\mathrm{O} 7^{\mathrm{iv}}-\mathrm{O} 7^{\mathrm{vi}}$ edges lying in the ( $\overline{1} 01$ ) plane, stack parallel to the $b$-axis direction by sharing $\mathrm{O} 3-\mathrm{O}^{\text {vi }}$ edges. $\mathrm{Ca} 1 / \mathrm{Eu} 1-$ and $\mathrm{Ca} 2 / \mathrm{Eu} 2-$ centred trigonal prism pairs share $\mathrm{O} 3-\mathrm{O}^{\mathrm{v}}$ edges and form trigonal prism layers in the ( $20 \overline{1}$ ) plane. Ca3/Eu3, Ca4/Eu4 and


Figure 4
The arrangement of $\mathrm{Ca} 1 / \mathrm{Eu} 1$-centred and $\mathrm{Ca} 2 / \mathrm{Eu} 2$-centred oxygen trigonal prisms in $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$.
$\mathrm{Ca} 5 / \mathrm{Eu} 5 / \mathrm{Sn} 5$ atoms are located between the trigonal prism layers (Fig. 3a). A similar arrangement of prism pairs is seen in the structure of B-form $\mathrm{Eu}_{2} \mathrm{O}_{3}$, where the layers of Eu1- and Eu2-centred prism pairs share vertices and form tunnels parallel to the $b$-axis direction. Eu3 atoms are located in sevenfold coordination sites in the tunnels.

## Experimental

The starting materials were powders of $\mathrm{Eu}_{2} \mathrm{O}_{3}(99.99 \%$ purity; Rare Metallic), $\mathrm{CaCO}_{3}$ ( $99.99 \%$ purity; Rare Metallic) and $\mathrm{SnO}_{2}$ ( $99.9 \%$ purity; Sigma-Aldrich). $\mathrm{Eu}_{2} \mathrm{O}_{3}$ and $\mathrm{SnO}_{2}$ powders were heated at 1273 K for 6 h before weighing. The powders were weighed and mixed in a Ca:Eu:Sn molar ratio of 1:3:1. The mixture was pressed into a pellet at 50 MPa and placed on a platinum-rhodium plate. The polycrystalline sample of $\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{Sn}_{0.5} \mathrm{O}_{7}$ was prepared by reaction sintering at 2073 K using an electric furnace in air. After heating at this temperature for 12 h , the sample was cooled to room temperature in the furnace. The growth of grains was observed in the sample. A colourless translucent single-crystal platelet was selected from the grains. The compositions of $\mathrm{Ca}, \mathrm{Eu}$ and Sn in the single-crystal were measured using a scanning electron microscope (SEM, Hitachi, S3500N) with an energy dispersive X-ray spectrometer (EDX, HORIBA, EMAX-500).

## Crystal data

$\mathrm{Ca}_{1.5} \mathrm{Eu}_{3} \mathrm{O}_{7} \mathrm{Sn}_{0.5}$
$M_{r}=687.35$
Monoclinic, $C 2 / m$
$a=22.8628$ (11) $\AA$
$b=3.6294$ (2) $\AA$
$c=9.0610$ (4) $\AA$
$\beta=107.9150(14)^{\circ}$
$V=715.41(6) \AA^{3}$

## Data collection

Rigaku R-AXIS RAPID
$\quad$ diffractometer
$\omega$ scans
Absorption correction: numerical
$\quad(N U M A B S ;$ Higashi, 1999)
$\quad T_{\min }=0.276, T_{\max }=0.719$

$$
\begin{aligned}
& Z=4 \\
& D_{x}=6.384 \mathrm{Mg} \mathrm{~m}^{-3} \\
& \text { Mo } K \alpha \text { radiation } \\
& \mu=28.75 \mathrm{~mm}^{-1} \\
& T=296.1 \mathrm{~K} \\
& \text { Platelet, colourless } \\
& 0.07 \times 0.05 \times 0.03 \mathrm{~mm}
\end{aligned}
$$

Rigaku R-AXIS RAPID
diffractometer
$\omega$ scans
Absorption correction: numerical
$T_{\text {min }}=0.276, T_{\text {max }}=0.719$

## Refinement

Refinement on $F^{2}$
$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.026$
$w R\left(F^{2}\right)=0.061$
$S=1.06$
945 reflections
73 parameters

$$
\begin{aligned}
& w=1 /\left[\sigma^{2}\left(F_{\mathrm{o}}^{2}\right)+4.2873 P\right] \\
& \text { where } P=\left(F_{\mathrm{o}}^{2}+2 F_{\mathrm{c}}^{2}\right) / 3 \\
& (\Delta / \sigma)_{\max }=0.001 \\
& \Delta \rho_{\max }=1.52 \mathrm{e}^{-3} \\
& \Delta \rho_{\min }=-1.42 \mathrm{e}^{-3}
\end{aligned}
$$

Table 1
Selected bond lengths ( $\AA$ ).

| Ca1/Eu1-O4 ${ }^{\text {i }}$ | 2.272 (6) | Ca3/Eu3-O2 | 2.513 (5) |
| :---: | :---: | :---: | :---: |
| Ca1/Eu1-O6 ${ }^{\text {ii }}$ | 2.367 (4) | Ca3/Eu3-O2 ${ }^{\text {iii }}$ | 2.541 (4) |
| Ca1/Eu1-O4 | 2.395 (5) | Ca4/Eu4-O4 | 2.250 (3) |
| Ca1/Eu1-O3 | 2.528 (4) | Ca4/Eu4-O5 | 2.264 (5) |
| Ca1/Eu1-O1 | 2.606 (7) | Ca4/Eu4-O3 | 2.291 (5) |
| $\mathrm{Ca} 2 / \mathrm{Eu} 2-\mathrm{O} 7^{\text {iii }}$ | 2.288 (3) | Ca4/Eu4-O2 | 2.580 (4) |
| $\mathrm{Ca} 2 / \mathrm{Eu} 2-\mathrm{O} 7^{\text {iv }}$ | 2.293 (5) | Ca4/Eu4-O6 | 3.311 (9) |
| Ca2/Eu2-O1 | 2.402 (6) | Ca5/Eu5/Sn5-O1 ${ }^{\text {v }}$ | 2.118 (3) |
| Ca2/Eu2-O3 | 2.488 (4) | Ca5/Eu5/Sn5-O6 | 2.160 (7) |
| Ca2/Eu2-O2 | 2.716 (5) | Ca5/Eu5/Sn5-O5 | 2.202 (5) |
| Ca3/Eu3-O7 | 2.213 (5) | Ca5/Eu5/Sn5-O6 ${ }^{\text {vi }}$ | 2.386 (9) |
| Ca3/Eu3-O5 | 2.293 (4) |  |  |

The highest peak and deepest hole in the final electron-density difference map were observed at ( $0.1437,0.0000,0.0666$ ), $0.87 \AA$ from atom O1, and at $(0.3523,0.0000,0.4679), 0.63 \AA$ from atom Eu4, respectively.

Data collection: PROCESS-AUTO (Rigaku/MSC, 2005); cell refinement: PROCESS-AUTO; data reduction: CrystalStructure (Rigaku/MSC, 2005); program(s) used to solve structure: SIR2004 (Burla et al., 2005); program(s) used to refine structure: SHELXL97 (Sheldrick, 1997); molecular graphics: ATOMS (Dowty, 1999); software used to prepare material for publication: SHELXL97.

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Supplementary data for this paper are available from the IUCr electronic archives (Reference: FA3035). Services for accessing these data are described at the back of the journal.

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